Title of the course: Models of set theory

Course instructor: Stevo Todorčević

Status of the course: non-obligatory

Number of ESPB points:

Prerequisites: none.

Aim of the course:

Students should get familiar with methods of constructing models of set theory (forcing and inner models).

Expected results of the course:

At the end of the course a student is expected to show understanding of covered material in set theory through presenting proofs of theorems and familiarity with basic methods in this area.

Syllabus:

Lectures:

Souslin problem. Trees. Diamond principle, and diamond plus. Transitive models of set theory. Relativization and absoluteness. Constructible sets and consistency of the theory ZFC+GCH. Complete Boolean algebras. Boolean-valued models. Generic extensions. Forcing. Independence of the Continuum hypothesis and Axiom of choice. Forcing and infinitary combinatorics. Applications of forcing. Measure problem and measurable cardinals.

Recommended literature:

- 1. Thomas Jech, Set Theory, Springer, 1997.
- 2. Kenneth Kunen, Set Theory: an Introduction to Independence Proofs, North-Holland, 1980.
- 3. Frank R. Drake: Set Theory: an Introduction to Large Cardinals, North-Holland, 1974.

| Number of teaching hours: | Lectures: | Tutorial: |
|---------------------------|-----------|-----------|
| Methods of teaching: | | |

Lectures, problem-solving, and student presentations.

Grade (maximum number of points 100)

Seminar or homework: 50 points.

Oral exam: 50 points.