# Study programme(s): Master in Mathematics Teaching (MP), Mathematics (MA)

#### Level: master

Course title: Topology (MA-02)

Lecturer: Miloš S. Kurilić

Status: obligatory

**ECTS**: 7

#### Requirements: none

#### Learning objectives

Consolidation of the knowledge concerning metric and topological spaces (obtained in courses in mathematical analysis) on a more general level. Getting new knowledge necessary for understanding several subjects (e.g. Functional analysis, Theory of measure and integration).

## Learning outcomes

*Minimal:* understanding of the corresponding parts of the theory of cardinal numbers, general topology and the theory of metric spaces performing an ability to prove the main theorems and to analyze a given topological space.

Desired: deeper understanding of the corresponding parts of the theory of cardinal numbers, general topology and the theory of metric spaces performing the ability to prove the main theorems, to analyze and investigate a given topological space, to understand the standard examples and counterexamples, and to apply the knowledge in other areas of mathematics.

## **Syllabus**

Theoretical instruction: Cardinal number. Theorems of Schroeder-Bernstein and Cantor. Infinite and countable sets. Continuum. Operations with cardinal numbers. Topological space. Base and sub-base. The second countable spaces. Lindelof's theorem. Neighbourhoods. Local base. First countable spaces. The interior, exterior, boundary and closure of a set. Derived set. Density. Separability. Separation axioms. The normality of metric spaces. Continuous functions. Completely regular spaces. Open and closed mappings and homeomorphisms. Invariants and topological properties. Subspace. Hereditary properties. Restriction. Embedding. Connectedness. Components. Pathwise connected spaces. Compactness. Mappings of compact spaces. Sequential and countable compactness. Compactness in metric spaces. Tychonov product. Multiplicative properties. Tychonov's theorem. The diagonal mapping theorem. Universal spaces. Metric spaces. Metric invariants. Completeness and completion of metric spaces. Metrizability. Urysohn metrization theorem.

*Practical instruction:* Analysis of several topological spaces through exercises.

# Literature

1. M. Kurilić, Osnovi opšte topologije, Univerzitet u N. Sadu, PMF, N. Sad, 1998.

2. LJ. Gajić, M. Kurilić, S. Pilipović, B. Stanković, Zbirka zadataka iz funkcionalne

analize, Univerzitet u N. Sadu, PMF, Novi Sad, 2000.

	Weekly teaching load						
	Lectures: 3	Exercises: 3	Other forms of teaching:-	Student research:-	-		
Teaching methodology Lectures: Theoretical basis. Exercises: analysis of several top							
	spaces through						

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spaces	through	exercises.
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Grading (maximum number of points 100)					
Pre-exam obligations	points	Final exam	points		
Activity during lectures	-	Written exam			
Practical classes	-	Oral exam	50		
Colloquia	50				